

AP Calculus AB

Monday, September 23, 2013

Test Friday over derivatives!

This week, we will learn the product rule, quotient rule, and chain rule.

You need to be here for ETEH every day! :) Donald??

**Bellwork:** Write the **EQUATION** of the tangent line to the graph of

$$f(-1) = 2 - 1 = -3 \quad f(x) = 2x - x^2$$

at  $x = -1$ . Using technology, graph  $f(x)$  and the tangent line on the same axes.

$$f'(x) = 2 - 2x$$

$f'(-1) = 4 \rightarrow$  This is the slope of the tangent line @  $x = -1$ .

Need point also  $(-1, \overset{f(-1)}{-3})$

$$y + 3 = 4(x + 1)$$

$$y = 4x + 1$$

Eqn of tan line @  $x = -1$ .

$$31) y = 3x^5(2x^2 + 2)$$

$$y = 6x^7 + 6x^5$$

$$32) y = x^4(x^5 + 3)$$

$$33) y = (-x^5 + 1) \cdot 5x^2$$

$$34) y = (4x^4 + 1) \cdot -x^4$$

$$y' = 42x^6 + 30x^4$$

$$33) y = -5x^7 + 5x^2$$

$$y' = -35x^6 + 10x$$

$$y = 3x^5(2x^2 + 2)$$

Use prod rule:

$$f = 3x^5 \quad g = 2x^2 + 2$$

$$f' = 15x^4 \quad g' = 4x$$

$$\frac{d}{dx}(f \cdot g) = f g' + g \cdot f'$$

$$y' = 3x^5 \cdot 4x + (2x^2 + 2) \cdot 15x^4$$

$$y' = 12x^6 + 30x^6 + 30x^4$$

$$y' = 42x^6 + 30x^4$$

$$40) y = (2 + 3x^{-5})(x^2 + 2)$$

Product Rule 1<sup>st</sup>:

$$f = 2 + 3x^{-5} \quad g = x^2 + 2$$

$$f' = -15x^{-6} \quad g' = 2x$$

$$y' = (2 + 3x^{-5})(2x) + (x^2 + 2)(-15x^{-6})$$

Simplify w/ algebra.....

$$y' = 4x + 6x^{-4} - 15x^{-4} - 30x^{-6}$$

$$y' = 4x - 9x^{-4} - 30x^{-6}$$

Now, same problem - expand (1<sup>st</sup>), then power rule

$$40) y = (2 + 3x^{-5})(x^2 + 2)$$

$$y = 2x^2 + 4 + 3x^{-3} + 6x^{-5}$$

$$y' = 4x - 9x^{-4} - 30x^{-6}$$

c) Find  $f'(x)$  if  $f(x) = (3x^2 - 2x + 5)(-5x^4 + 2x^3 - 7x^2 + x + 2)$

$$f'(x) = (3x^2 - 2x + 5)(-20x^3 + 6x^2 - 14x + 1) + (-5x^4 + 2x^3 - 7x^2 + x + 2)(6x - 2)$$

Use the chart to find  $h'(4)$

$f(4)$	$f'(4)$	$g(4)$	$g'(4)$
-8	3	$3\pi$	4

31)  $h(x) = 5f(x) - \frac{2}{3}g(x)$

32)  $h(x) = 3 + 8f(x)$

33)  $h(x) = f(x)g(x)$

31)

$$h'(x) = 5 \cdot f'(x) - \frac{2}{3} \cdot g'(x)$$

$$h'(4) = 5 \cdot f'(4) - \frac{2}{3} \cdot g'(4)$$

Go to chart

$$h'(4) = 5 \cdot 3 - \frac{2}{3} \cdot 4$$

$$h'(4) = \frac{45}{3} - \frac{8}{3}$$

$$h'(4) = \frac{37}{3}$$

33)

$$h'(x) = f \cdot g' + g \cdot f'$$
$$h'(4) = f(4) \cdot g'(4) + g(4) \cdot f'(4)$$
$$-8(4) + 3\pi \cdot 3$$
$$-32 + 9\pi$$

$$A'(t) = 34 + 12t$$

$$l(t) \cdot w'(t) + w(t) \cdot l'(t) = A'(t) \quad \star$$

Create a table to investigate the relationship between  $w(t)$ ,  $l(t)$ ,  $w'(t)$ ,  $l'(t)$  and  $A'(t)$ .

$$A(t) = w(t) \cdot l(t)$$

$$A'(t) = l(t) \cdot w'(t) + w(t) \cdot l'(t)$$

PRODUCT Rule

OR

$$\frac{d}{dx} [f \cdot g] = f \cdot g' + g \cdot f'$$