

AP Calculus AB

Wednesday, October 16, 2013

10) Determine the concavity of the graph of

$$f(x) = 3 \sin(x) + 4 (\cos(x))^2$$

at $x = \pi$.

- a) 8
- b) -10
- c) 4
- d) -8
- e) -6

Flashcard:

concavity

Second deriv.

tangent

1st deriv

$$f(x) = 3 \sin x + 4 \cos^2 x$$

$$f'(x) = 3 \cos x + 8 \cos x \cdot (-\sin x)$$

$$f''(x) = -3 \sin x + 8 \cos x (-\cos x) + (-\sin x)(-8 \sin x)$$

$$f''(x) = -3 \sin x - 8 \cos^2 x + 8 \sin^2 x$$

$$f''(\pi) = -3 \sin \pi - 8 (\cos \pi)^2 + 8 (\sin \pi)^2$$

$$f''(\pi) = 0 - 8(-1)^2 + 8(0)^2$$

$$f''(\pi) = -8 \quad \text{D}$$